

# **Review of Lecture 6**

- Introduced the various form of first law and the State principle
- Introduced the ideal gas equation of state and the definition of specific heats. Learnt that u, h,  $c_p$  and  $c_v$  are only functions of temperature
- Derived the process relation for adiabatic frictionless process in ideal gas with constant specific heats
- Solved a few problems illustrating work and first law.
- Today, we shall build the concepts involving properties of water substance.



### **Properties of Pure Substances - II**

- Triple line p = 611 Pa, T = 0.01 °C
- Critical Point  $p = 22.09 \text{ MPa}, T = 374.14 \text{ }^{\circ}\text{C}$
- Water contracts on melting and  $T_{\text{melt}}$  decreases with increase in  $\boldsymbol{p}$
- Other substances that expand on Melting, the  $T_{\rm melt}$  increases with increase in p
- During phase change, p and T are not independent
- The solid-liquid transformation and solid-vapour transformation are not very useful in power generation applications and hence will not be discussed further.

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# **Properties of Pure Substances - IV**

#### Definitions

- Saturated temperature is the temperature at which change of phase occurs at constant pressure. It is a function of pressure.  $T_{sat} = T_{sat}(p)$
- **Saturated pressure** is the pressure at which change of phase occurs at constant temperature. It is a function of temperature. p<sub>sat</sub> = p<sub>sat</sub>(T)
- Subcooled Liquid is the state when  $T < T_{sat}(p)$
- **Superheated vapour** is the state is when  $T > T_{sat}(p)$
- The state is wet,  $T = T_{sat}$ ,  $p = p_{sat}$  and a mixture of vapour and liquid is simultaneously present.

# Steam Tables - I

- Ideal gas temperature holds, when p <<  $p_c, \ T >> T_{sat}$
- Equation of state of a real substance is quite complicated.
- These are tabulated in the form of tables.
- Generally this table is in three forms
  - Saturated Tables
  - Superheated vapour Table
  - Compressed liquid Table.
- The last one is often skipped and Incompressible model is used.

# **Steam Tables - II**

- For every  $T_{triple point} < T < T_{critical}$ , there exists a  $p_{sat}$
- The saturated liquid properties are denoted by the subscript **f** and the saturated vapour properties are denoted by the subscript **g**
- In saturated pressure table, for every  $p_{sat}$ , the corresponding  $T_{sat}$ ,  $v_f$ ,  $v_g$ ,  $u_f$ ,  $u_g$ ,  $h_f$ ,  $h_g$ ,  $h_{fg} s_f$ ,  $s_{fg}$  and  $s_g$  are tabulated
- In saturated temperature table, for every  $T_{sat}$ , the corresponding  $p_{sat}$ ,  $v_f$ ,  $v_g$ ,  $u_f$ ,  $u_g$ ,  $h_f$ ,  $h_g$ ,  $h_{fg}$ ,  $s_f$ ,  $s_{fg}$  and  $s_g$  are tabulated

# **Steam Tables - III**

- In superheated steam table, for every pressure, the values of v, u, h and s are tabulated at regular intervals of temperature for  $T > T_{sat}$
- Thus the properties of the gas and liquid phase in saturated state and the properties of gas at superheated vapour state can be obtained
- When a mixture of two phases exists, we define a parameter **x**, which is defined as the fraction of mass of vapour in the mixture. This parameter is called dryness fraction or quality

## **Steam Tables - IV**

- The properties of two-phase mixture is estimated using the dryness fraction as follows
- Consider, Volume of two-phase mixture, V

$$V = V_{f} + V_{g} = m_{f} v_{f} + m_{g} v_{g}$$
  

$$\Rightarrow v = \frac{V}{m_{f} + m_{g}} = \frac{m_{f} v_{f} + m_{g} v_{g}}{m_{f} + m_{g}}$$
  

$$\Rightarrow v = \frac{m_{f}}{m_{f} + m_{g}} v_{f} + \frac{m_{g}}{m_{f} + m_{g}} v_{g}$$
  

$$\Rightarrow v = (1 - x) v_{f} + x v_{g}$$

# Steam Tables - V • In a similar fashion all the specific properties will be dryness fraction weighted. $u = (1-x)u_f + xu_g \qquad h = (1-x)h_f + xh_g$ $s = (1-x)s_f + xs_g$ • From the above we can write, $x = \frac{v - v_f}{v_g - v_f} = \frac{u - u_f}{u_g - u_f} = \frac{h - h_f}{h_g - h_f} = \frac{s - s_f}{s_g - s_f}$

#### Incompressible liquid model

- For incompressible substances, u = u(T), v = v(T)and  $s(T) = s_f(T)$
- Hence we can estimate u, v and s for liquids as u (T) =  $u_f(T)$ , v (T) =  $v_f(T)$  and s (T) =  $s_f(T)$
- Finally, h(T) can be estimated as

 $h(p,T) = u_f(T) + pv_f(T)$ 

