

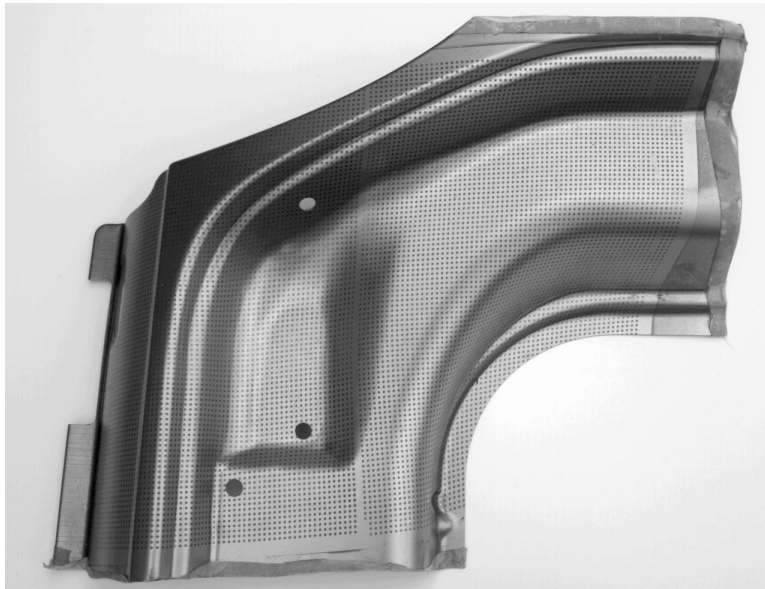
# Sheet Metal Forming - 1

# Outline

- Introduction
- Key Factors
- Sheet Bending

# Introduction

- Sheet metal: metallic sheet typically  $< 6$  mm thick
- Large surface area/volume ratio
- Applications: auto body parts, beverage cans, utensils



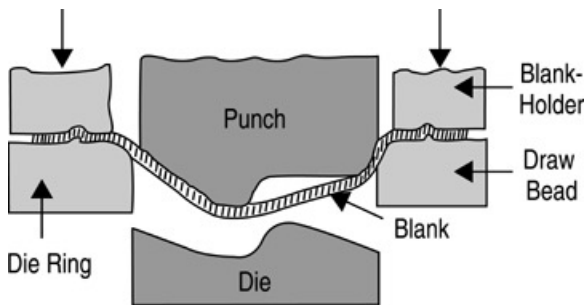
**Stamped sheet metal part**



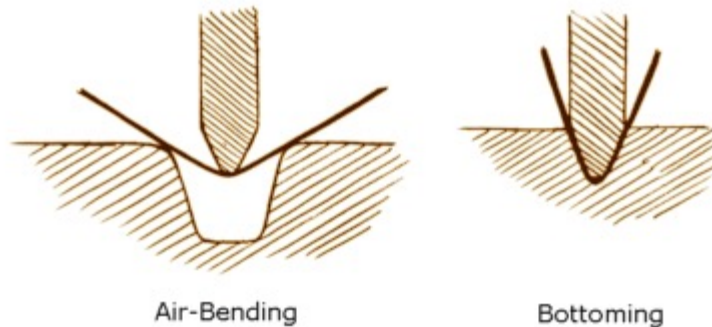
**Aluminum can**

# Introduction

- Sheet forming processes: sheet bending, stamping, deep drawing, shearing, etc.
- Constant volume processes
- Basic deformation modes: bending and stretching



**Deep drawing**



**Metal bending machine**

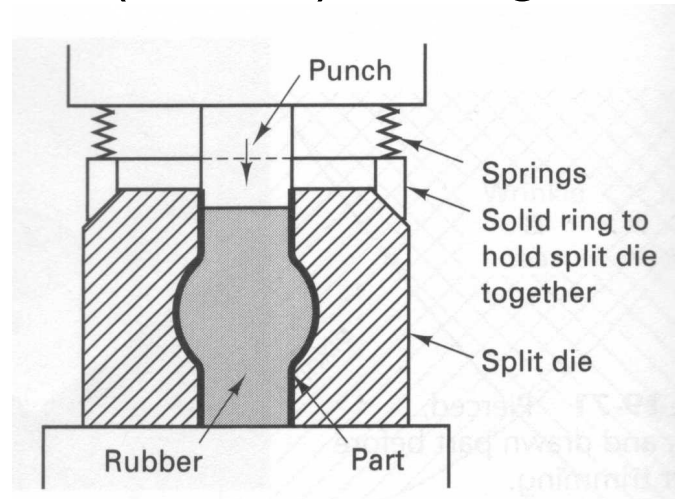
# Stamping



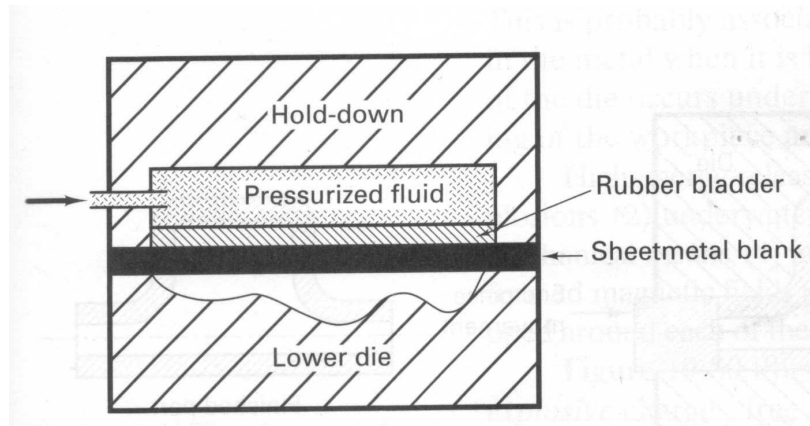
<http://video.google.com/videoplay?docid=-6082773547960703710&q=metal+stamping&total=70&start=0&num=10&so=0&type=search&plindex=4>

# Process Variations

- Forming with flexible (rubber) tooling



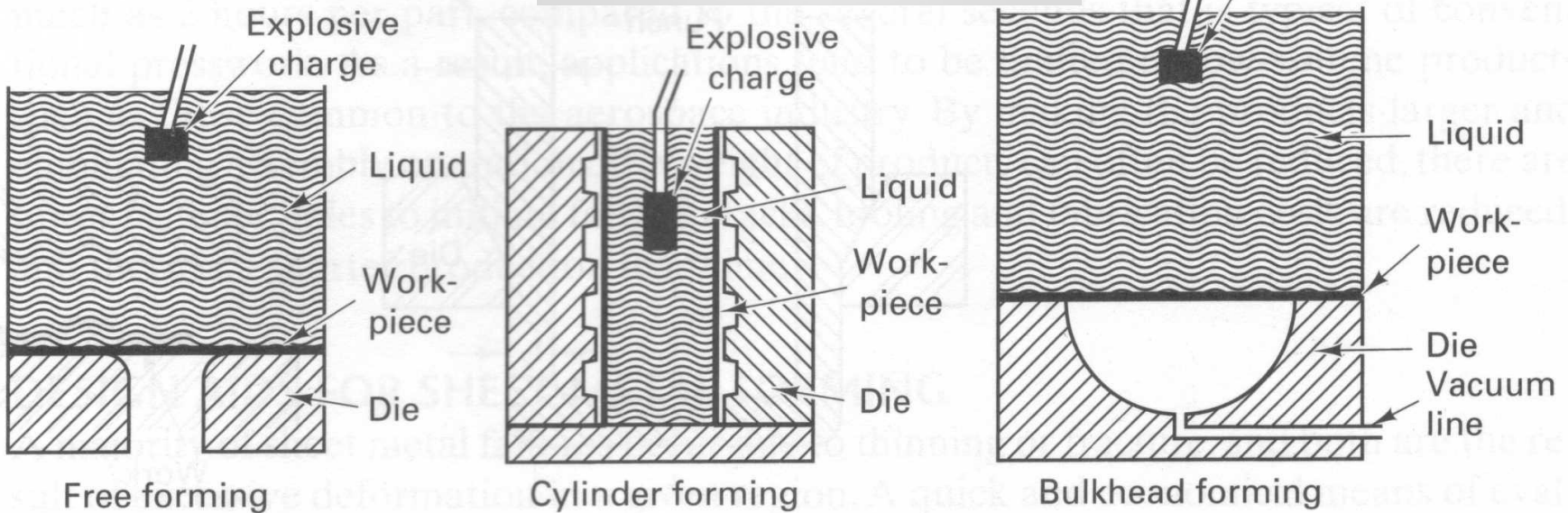
- Hydroforming



Source: DeGarmo, Black, Kohser, 9<sup>th</sup> Ed., 2003

# Process Variations

- Explosive forming



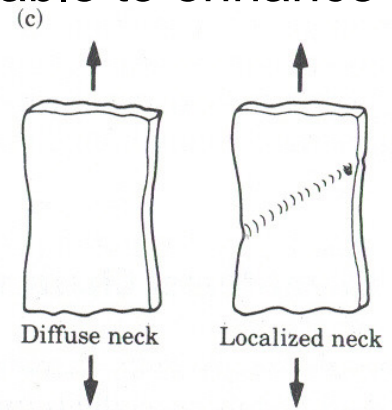
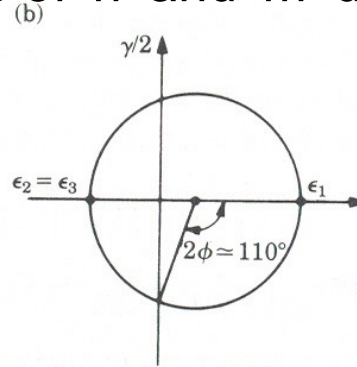
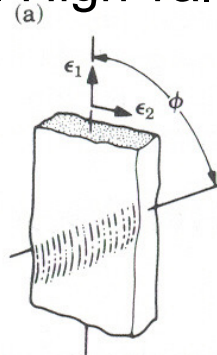
Source: DeGarmo, Black, Kohser, 9<sup>th</sup> Ed., 2003

# Key Factors

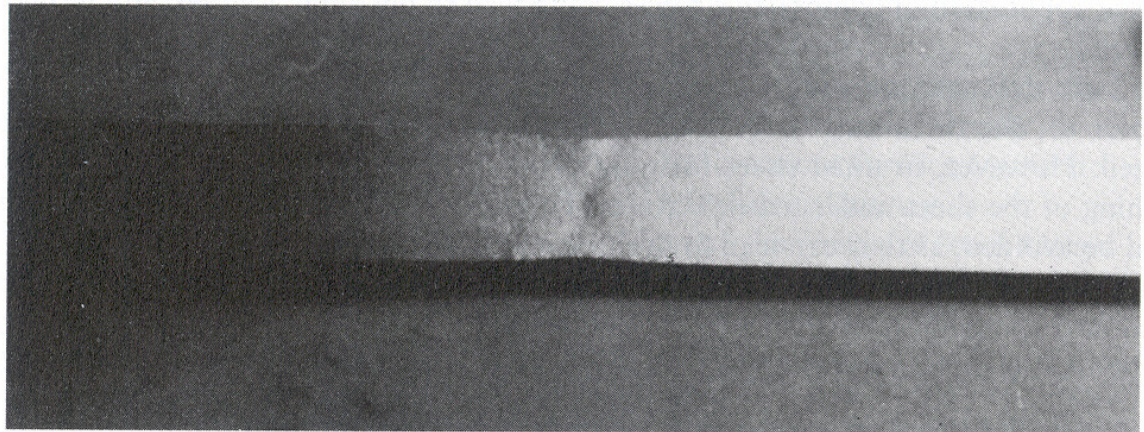
- Elongation: tensile loads in stretching can cause necking → limits uniform elongation. Sheet metal specimens tend to undergo “localized necking”. High values of ‘ $n$ ’ and ‘ $m$ ’ desirable to enhance total elongation.

$$\sigma = K \varepsilon^n$$

$$\sigma = C \dot{\varepsilon}^m$$



(d)



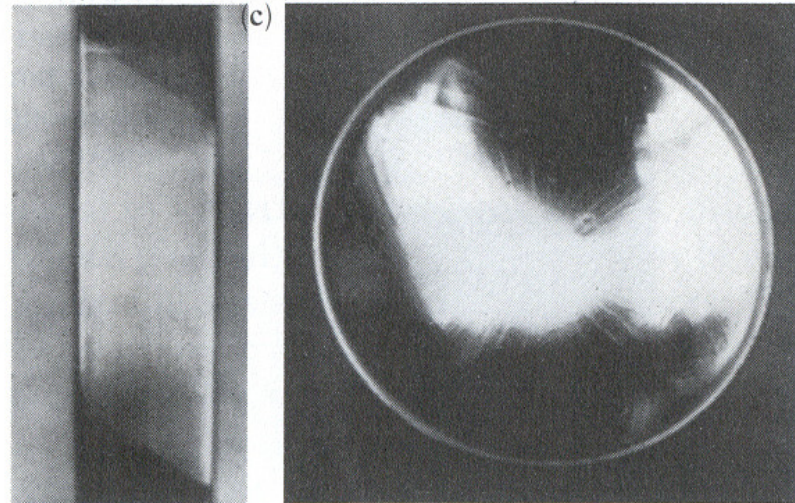
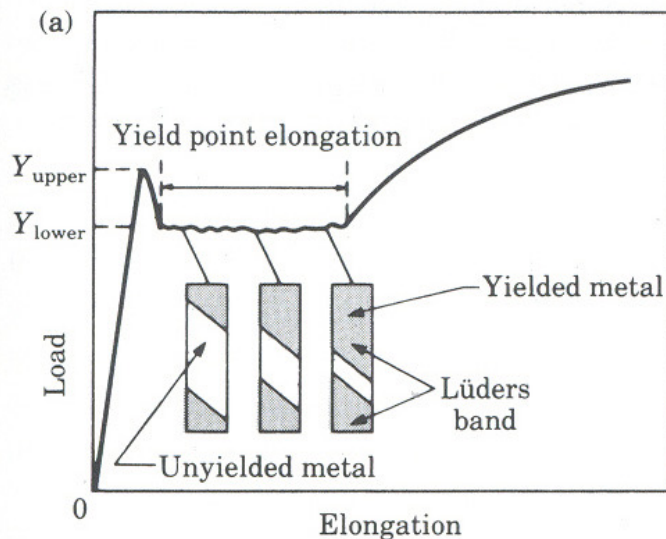
$n \uparrow \rightarrow$  uniform elongation  $\uparrow$   
 $m \uparrow \rightarrow$  post-uniform elongation  $\uparrow$

Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003



# Key Factors

- Yield-Point Elongation: Yield point elongation is a function of the strain-rate and the grain size; increases as strain-rate $\uparrow$  and grain size $\downarrow$
- Characteristic of low carbon steels

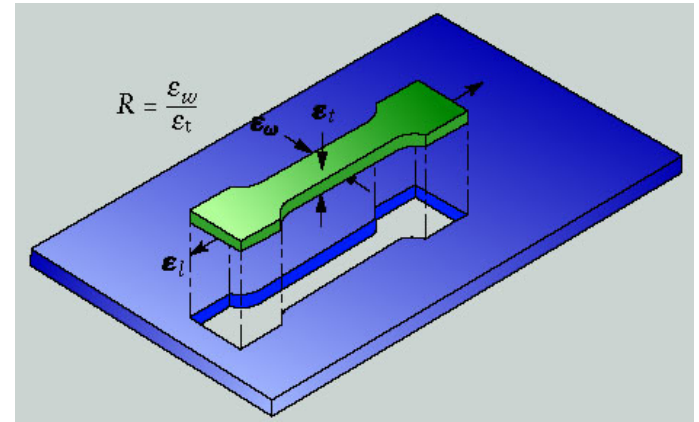


Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Key Factors

- Anisotropy: directional properties (of rolled sheet)
- Causes
  - crystallographic (from preferred grain orientation)
  - mechanical fibering (impurities, inclusions, etc. aligned in one direction)
- Significance: can lead to defects such as earing, wrinkling, or fracture
- Severity of directionality measured by plastic strain ratio,  $R$ , or normal anisotropy

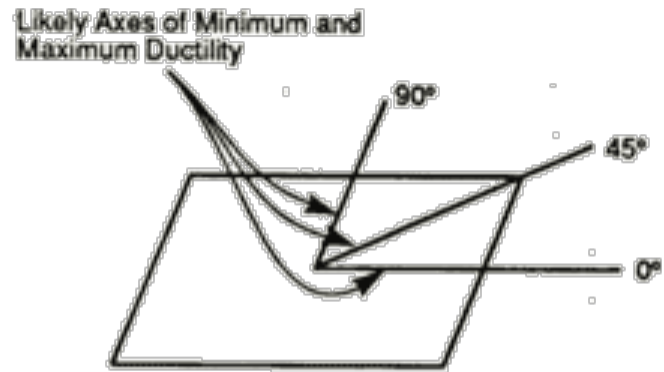
$$R = \frac{\text{width strain}}{\text{thickness strain}} = \frac{\epsilon_w}{\epsilon_t} = \frac{\ln\left(\frac{w_0}{w_f}\right)}{\ln\left(\frac{t_0}{t_f}\right)} = \frac{\ln\left(\frac{w_0}{w_f}\right)}{\ln\left(\frac{w_f l_f}{w_0 l_0}\right)}$$



# Key Factors

- $R$  varies with direction of tensile stress application relative to sheet rolling direction
- Average normal anisotropy,  $\bar{R}$

$$\bar{R} = \frac{R_{0^\circ} + 2R_{45^\circ} + R_{90^\circ}}{4}$$



- Planar anisotropy,  $\Delta R$

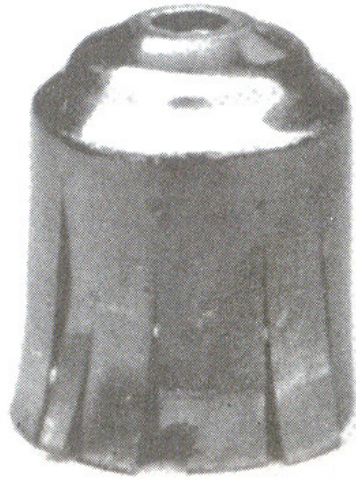
$$\Delta R = \frac{R_{0^\circ} - 2R_{45^\circ} + R_{90^\circ}}{2}$$

Directionality in Properties of a Rolled Sheet

$R_{\theta=0, 45, 90}$  are the normal anisotropies in the sheet at the specified angles relative to the rolling direction of sheet

# Key Factors

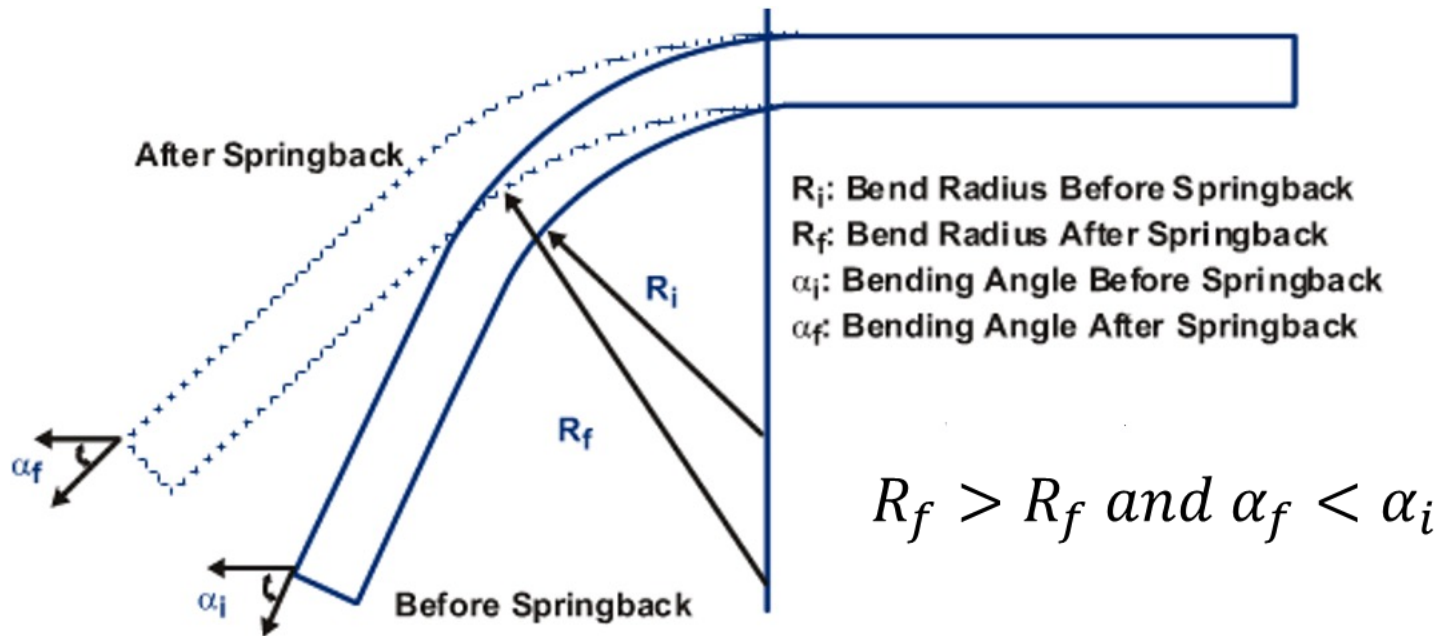
- Grain size: impacts mechanical properties and appearance of surface of sheet
  - Finer grain size → stronger the sheet, smoother surface
- Residual stresses: due to non-uniform deformation
  - Tensile stresses → stress corrosion cracking, part distortion



Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Key Factors

- Springback: elastic recovery of sheet; common in bending operations



# Key Factors

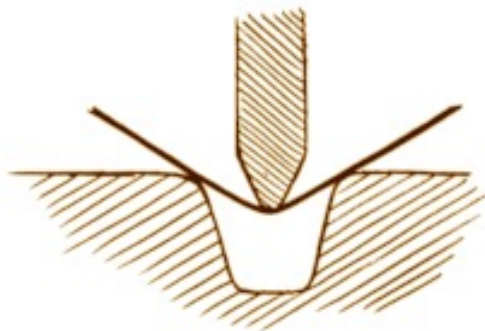
- Wrinkling: due to compressive stresses acting in the plane of the sheet (common in deep drawing)



Source: [www2.thefabricator.com](http://www2.thefabricator.com)

# Sheet Metal Bending

- Process used to create parts with bends in them
- Bending also enhances rigidity of part
- Process carried out on a press brake machine



Air-Bending

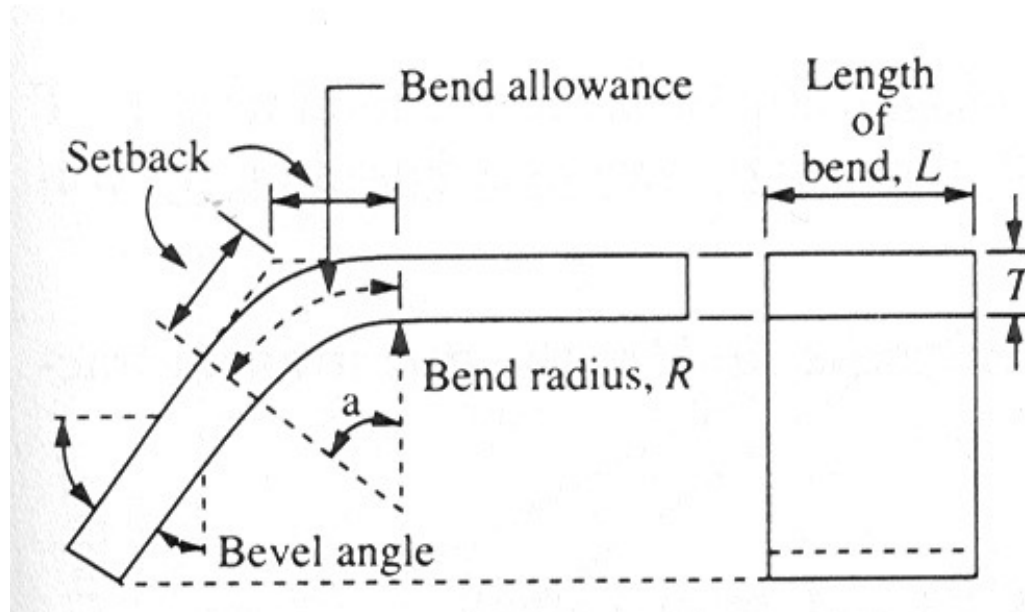


Bottoming



**Metal bending machine**

# Sheet Metal Bending



Engineering strains (theoretical):

$$e_o = e_i = \frac{1}{\left(\frac{2R}{T}\right) + 1}$$

$e_i$  = strain in inner fiber;  $e_o$  = strain in outer fiber

$\therefore$  as  $\frac{R}{T} \downarrow$   $e_o \uparrow \rightarrow$  cracking on outer bend surface

Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003



# Sheet Metal Bending

- Minimum bend radius: expressed as an integer ( $n$ ) multiple of the sheet thickness  $T$  i.e.  $nT$
- Determined experimentally
- Theoretically,

$$\text{Min. } \frac{R}{T} = \frac{50}{r} - 1$$

$r = \% \text{ reduction in area in a tension test}$

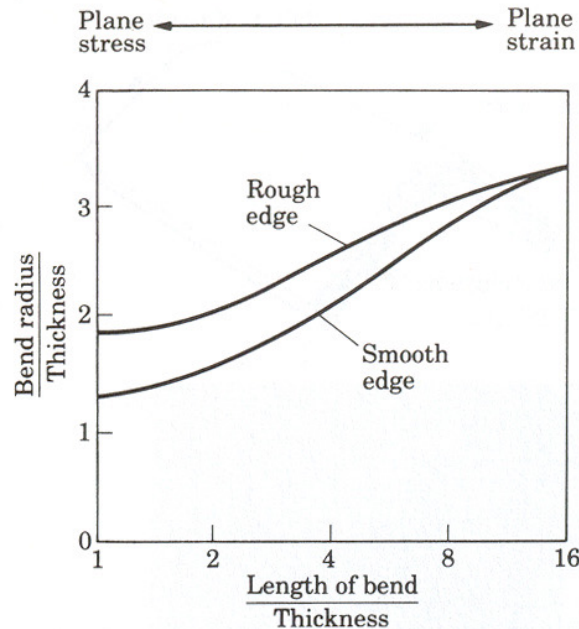
Expression for min. bend radius derived by equating true strain at fracture in tension,  $\varepsilon_f = \varepsilon_0$ , true strain in outer fiber of bent sheet

$$\text{Note that } \varepsilon_f = \ln\left(\frac{A_0}{A_f}\right) = \ln\left(\frac{100}{100 - r}\right)$$

$$\text{and } \varepsilon_0 = \ln(1 + e_0) = \ln\left(\frac{R + T}{R + 0.5T}\right)$$

# Factors Affecting Bendability

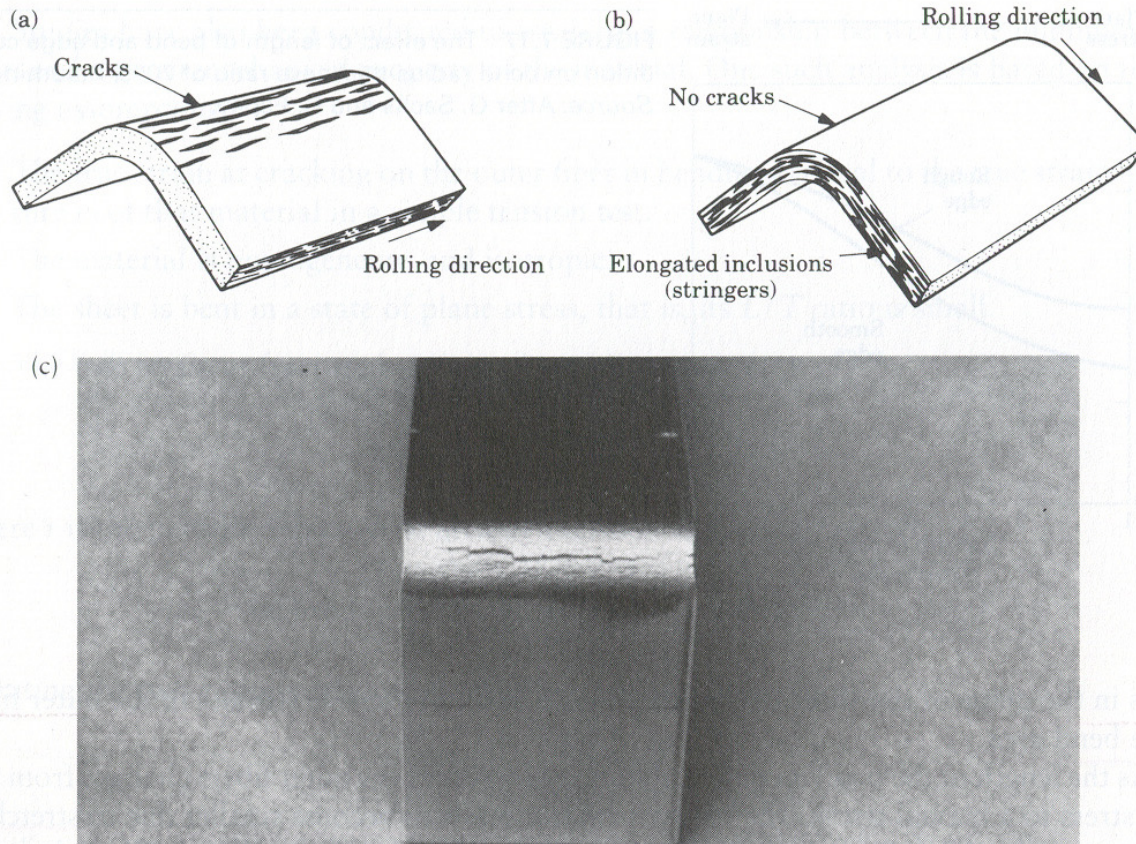
- Bendability can be enhanced by heating, applying compressive stresses in plane of sheet
- As  $L \uparrow \rightarrow$  state of strain in outer fiber changes from uniaxial to biaxial  $\rightarrow$  decreases ductility and the Min. R/T ratio  $\uparrow$



Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Factors Affecting Bendability

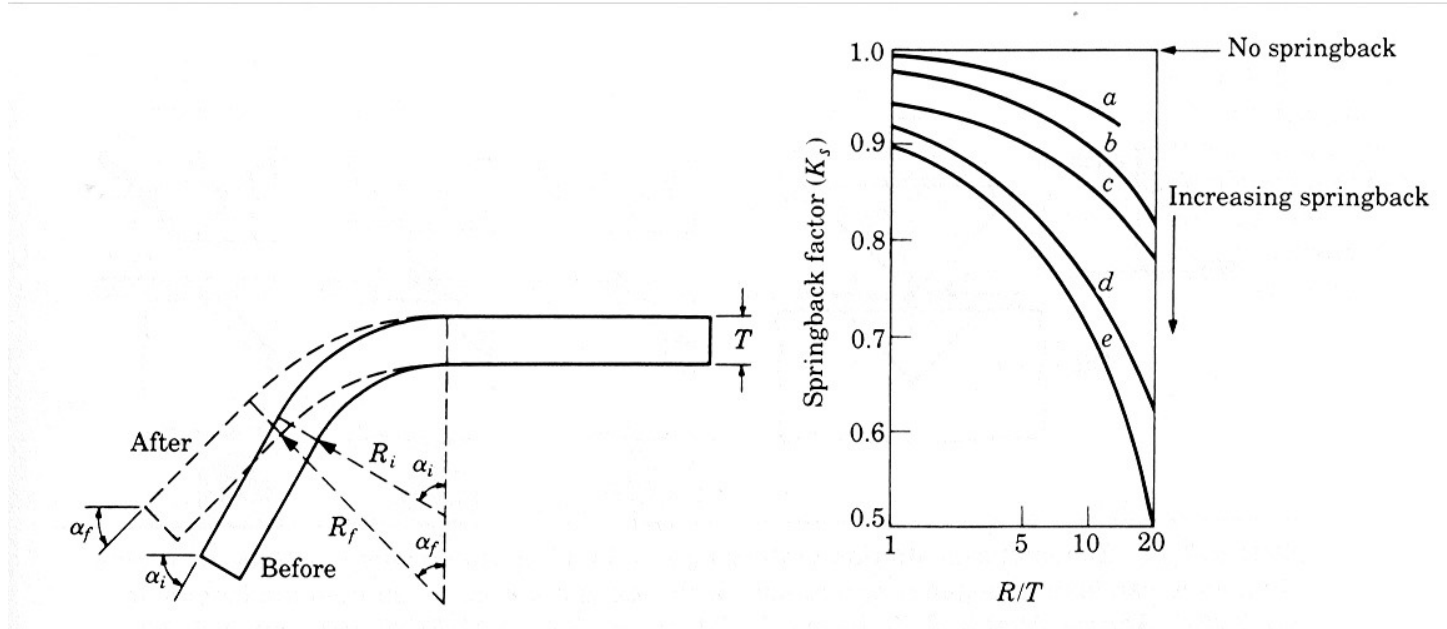
- Direction of Anisotropy



Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Factors Affecting Bendability

- Springback: results in larger bend radius and smaller bend angle,  $\alpha$



Springback factor,  $K_s$

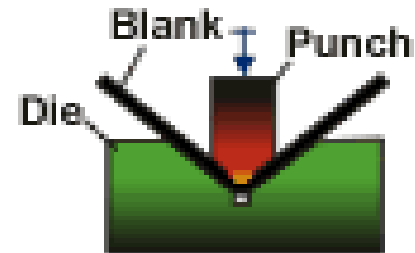
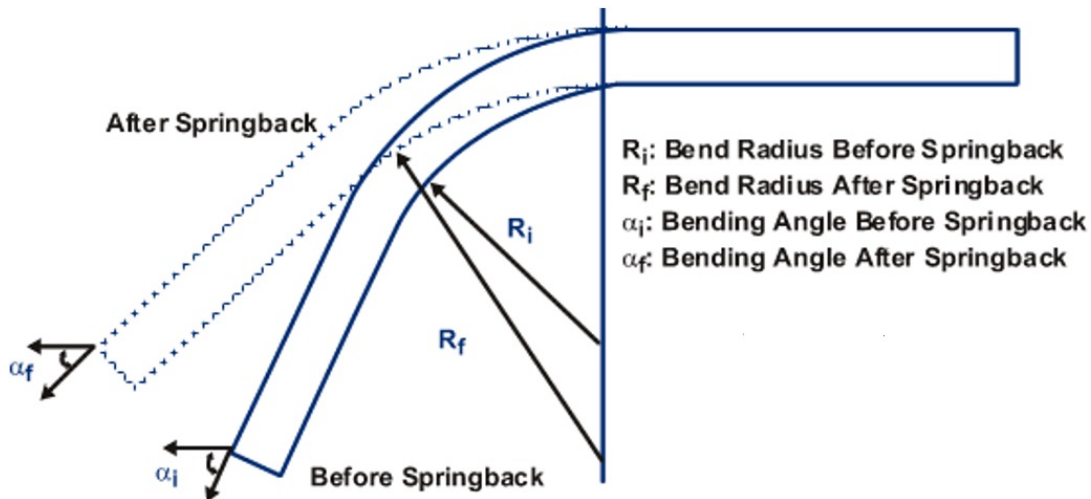
$$K_s = \frac{\alpha_f}{\alpha_i} = \frac{(2R_i/T) + 1}{(2R_f/T) + 1} \quad \frac{R_i}{R_f} = 4 \left( \frac{R_i Y}{ET} \right)^3 - 3 \left( \frac{R_i Y}{ET} \right) + 1$$

Where  $Y$  is the yield strength and  $E$  is the Young's modulus

Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Factors Affecting Bendability

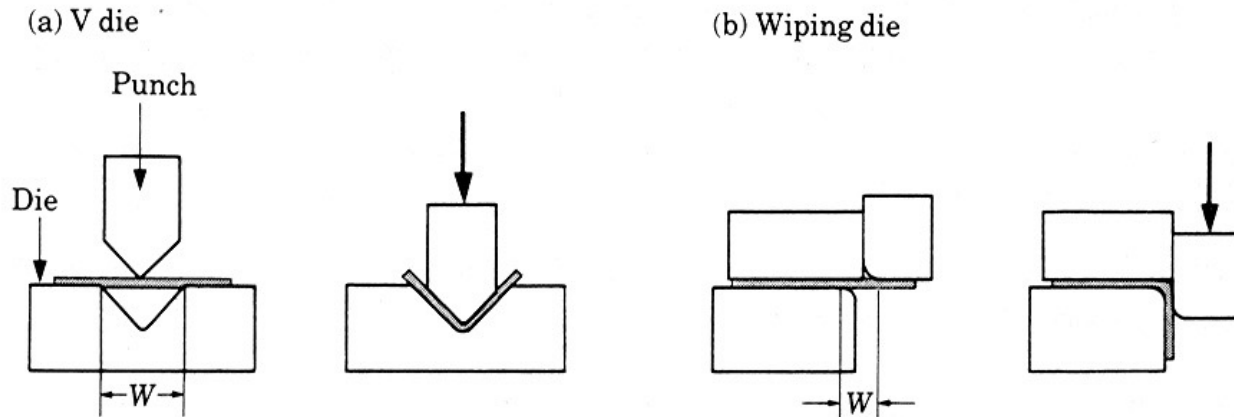
- Springback compensation methods
  - Overbending
  - Heating → lowers yield strength
  - Coining
  - Stretch bending



Coining

$$R_f > R_i \text{ and } \alpha_f < \alpha_i$$

# Bending Force Calculation



- Max. bending force,  $P_{\max}$  (neglecting friction)

$$P_{\max} = \frac{kYLT^2}{W} \approx k \frac{(UTS)LT^2}{W}$$

$k = 1.2 \sim 1.3$  for V dies

$k = 0.3$  for wiping

$k = 2.4$  for U dies

Source: Kalpakjian & Schmidt, 4<sup>th</sup> Ed., 2003

# Summary

- Sheet metal basics
- Key factors
- Sheet metal bending