

Common Laplace Transform Pairs

Time Domain Function		Laplace Domain Function
Name	Definition*	
Unit Impulse	$\delta(t)$	1
Unit Step	$\gamma(t)^\dagger$	$\frac{1}{s}$
Unit Ramp	t	$\frac{1}{s^2}$
Parabola	t^2	$\frac{2}{s^3}$
Exponential	e^{-at}	$\frac{1}{s+a}$
Asymptotic Exponential	$\frac{1}{a}(1-e^{-at})$	$\frac{1}{s(s+a)}$
Dual Exponential	$\frac{1}{b-a}(e^{-at} - e^{-bt})$	$\frac{1}{(s+a)(s+b)}$
Asymptotic Dual Exponential	$\frac{1}{ab} \left[1 + \frac{1}{a-b} (be^{-at} - ae^{-bt}) \right]$	$\frac{1}{s(s+a)(s+b)}$
Time multiplied Exponential	te^{-at}	$\frac{1}{(s+a)^2}$
Sine	$\sin(\omega_0 t)$	$\frac{\omega_0}{s^2 + \omega_0^2}$
Cosine	$\cos(\omega_0 t)$	$\frac{s}{s^2 + \omega_0^2}$
Decaying Sine	$e^{-at} \sin(\omega_d t)$	$\frac{\omega_d}{(s+a)^2 + \omega_d^2}$
Decaying Cosine	$e^{-at} \cos(\omega_d t)$	$\frac{s+a}{(s+a)^2 + \omega_d^2}$
Generic Oscillatory Decay	$e^{-at} \left[B \cos(\omega_d t) + \frac{C - aB}{\omega_d} \sin(\omega_d t) \right]$	$\frac{Bs + C}{(s+a)^2 + \omega_d^2}$
Prototype Second Order Lowpass, underdamped	$\frac{\omega_0}{\sqrt{1-\zeta^2}} e^{-\zeta\omega_0 t} \sin(\omega_0 \sqrt{1-\zeta^2} t)$	$\frac{\omega_0^2}{s^2 + 2\zeta\omega_0 s + \omega_0^2}$
Prototype Second Order Lowpass, underdamped - Step Response	$1 - \frac{1}{\sqrt{1-\zeta^2}} e^{-\zeta\omega_0 t} \sin(\omega_0 \sqrt{1-\zeta^2} t + \phi)$ $\phi = \tan^{-1} \left(\frac{\sqrt{1-\zeta^2}}{\zeta} \right)$	$\frac{\omega_0^2}{s(s^2 + 2\zeta\omega_0 s + \omega_0^2)}$

*All time domain functions are implicitly=0 for t<0 (i.e. they are multiplied by unit step, $\gamma(t)$).

$\dagger u(t)$ is more commonly used for the step, but is also used for other things. $\gamma(t)$ is chosen to avoid confusion (and because in the Laplace domain it looks a little like a step function, $\Gamma(s)$).